

## Problem

- Certain assemblies require fine dexterity
- Changing manufacturing processes prevent the use of traditional robotic systems
- Current robotics systems cannot adapt to operator variability
- **Goal:** To recognize human activity for robotic assistance in human-robot collaborative tasks

## Sample Scenario: Assembly of a Motor

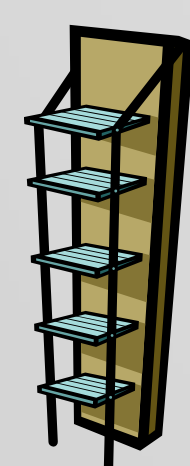
**Problem:** To assemble a motor consisting of multiple parts

- Labor is divided between a robot assistant and a human agent.
  - Assembly is performed by the human agent
  - Part/tool delivery is performed by a robot assistant
- Different assemblies require different tools and parts
- Tools and parts are transported to the human agent from a storage container
- Work space and tools are limited - Only one tool and part maybe checked out from the storage container at any point in time

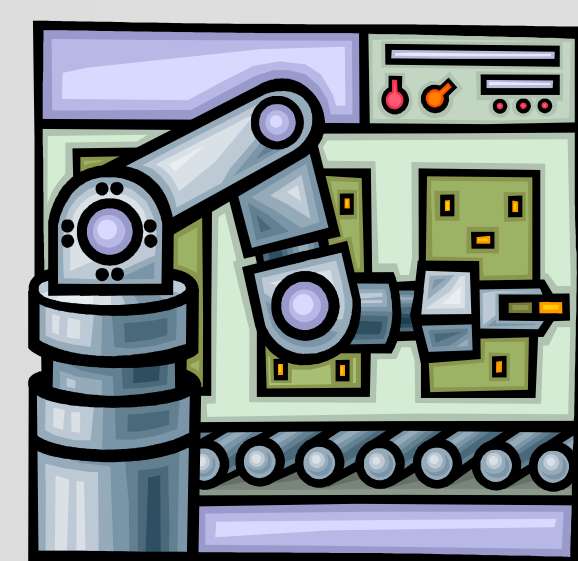


- Fine dexterity motions
- Assemble individual parts
- Limited work space

### Tools and Parts

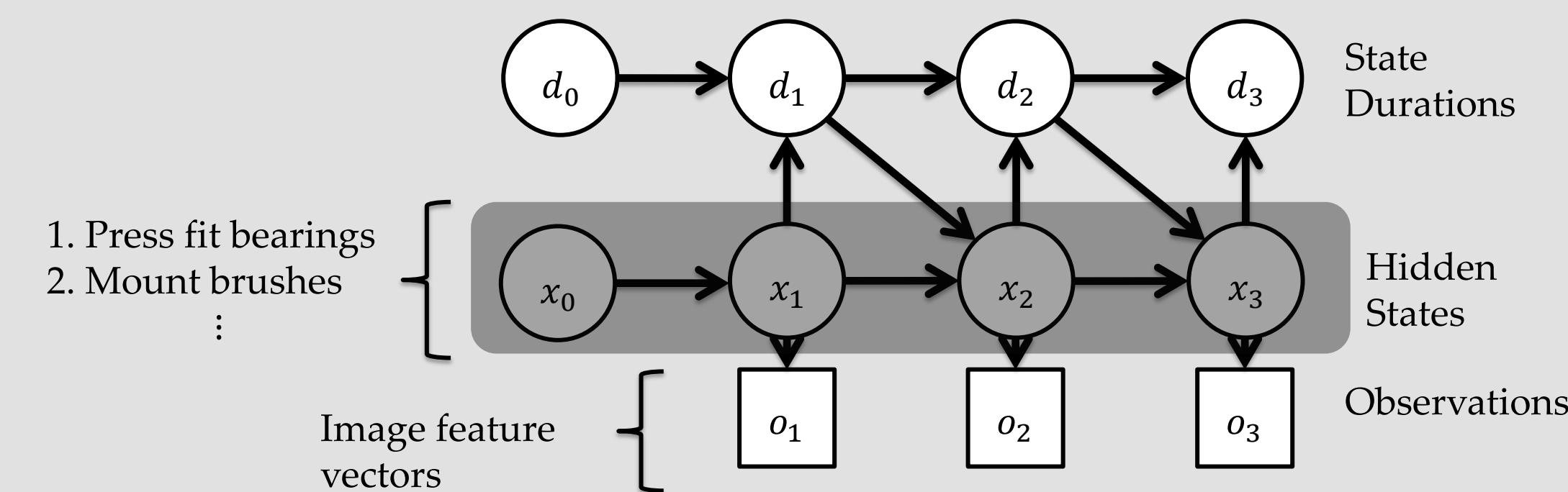


### Robot Assistant

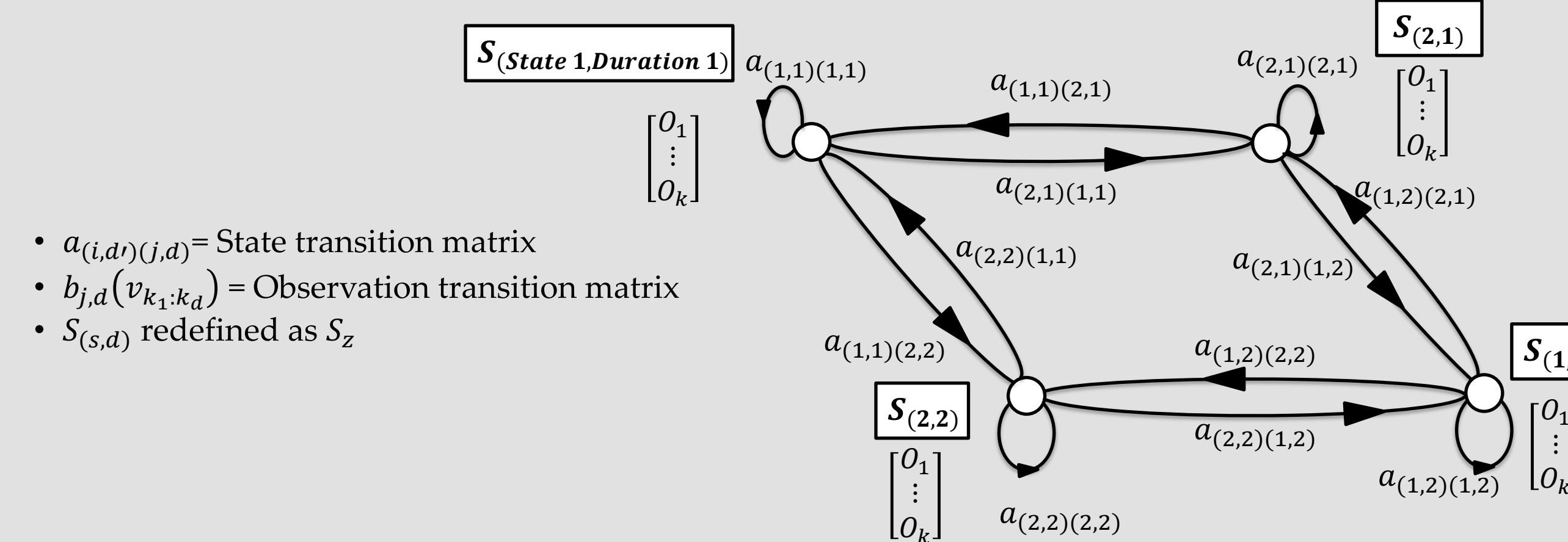


- A maximum of one tool and part may be taken at a time
- Delivers and receives tools and parts from human agent

## Hidden Semi-Markov Model

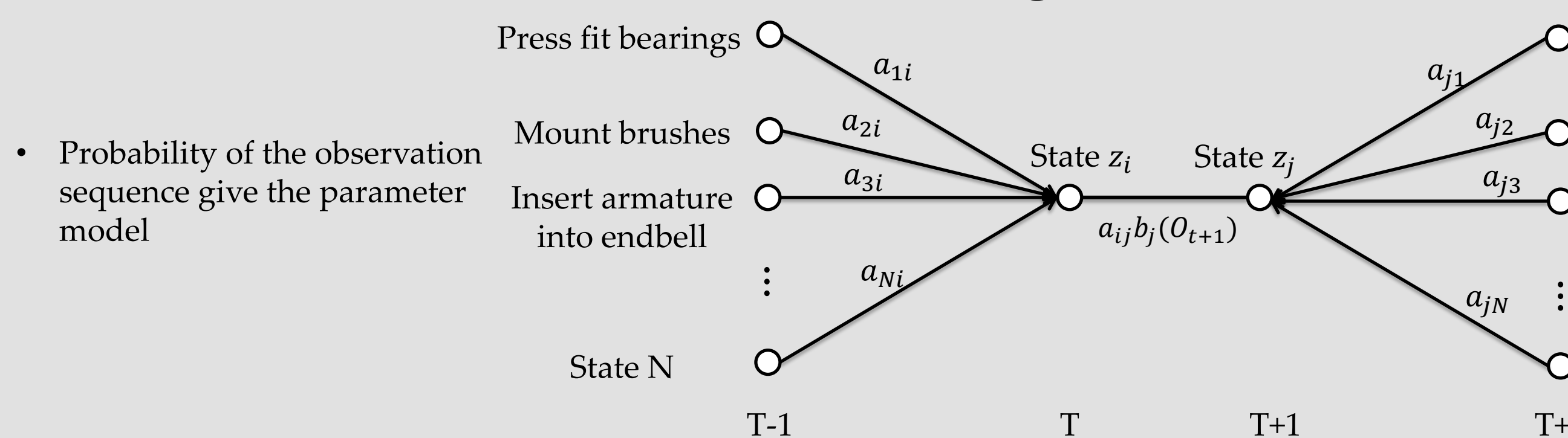


## Model Parameters



- $a_{(i,d_r)(j,a)}$  = State transition matrix
- $b_{j,a}(v_{k_1:k_d})$  = Observation transition matrix
- $S_{(s,a)}$  redefined as  $S_z$

## Forward-Backward Algorithm



- Probability of the observation sequence give the parameter model

## Parameter Estimation using Baum-Welch

$$\text{Probability of being in } S_i \text{ at } t \text{ and } S_j \text{ at } t+1 \quad \xi_t(i,j) = \frac{\alpha_t(i)a_{ij}b_j(o_{t+1})\beta_{t+1}(j)}{\sum_{i=1}^N \sum_{j=1}^N \alpha_t(i)a_{ij}b_j(o_{t+1})\beta_{t+1}(j)}$$

$$\text{Probability of being in } S_i \text{ at } t \text{ given the observation sequence} \quad \gamma_t(i) = \sum_{j=1}^N \xi_t(i,j)$$

Initial state distribution

$$\bar{\pi}_i = \gamma_1$$

$$\frac{\text{Expected \# of transitions from state } S_{z_i} \text{ to } S_{z_j}}{\text{Expected \# of transitions from state } S_{z_i}}$$

$$\bar{a}_{ij} = \frac{\sum_{t=1}^{T-1} \xi_t(i,j)}{\sum_{t=1}^{T-1} \gamma_t(i)}$$

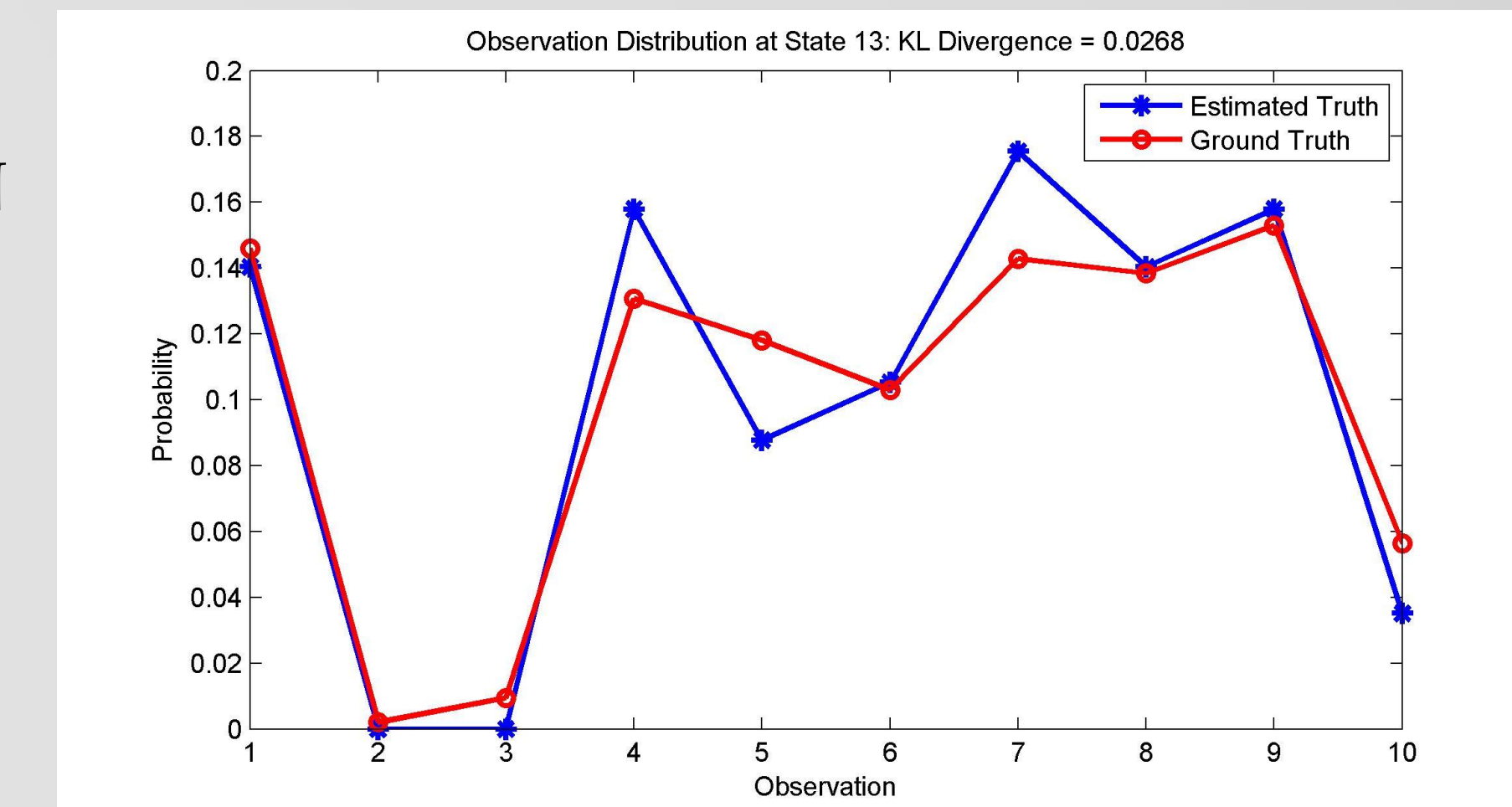
$$\frac{\text{Expected \# of times in } S_{z_j} \text{ and observing } v_k}{\text{Expected \# of times in state } S_{z_j}}$$

$$\bar{b}_j(k) = \frac{\sum_{t=1}^T \gamma_t(j) \cdot \mathbb{1}_{\{o_t = v_k\}}}{\sum_{t=1}^T \gamma_t(j)}$$

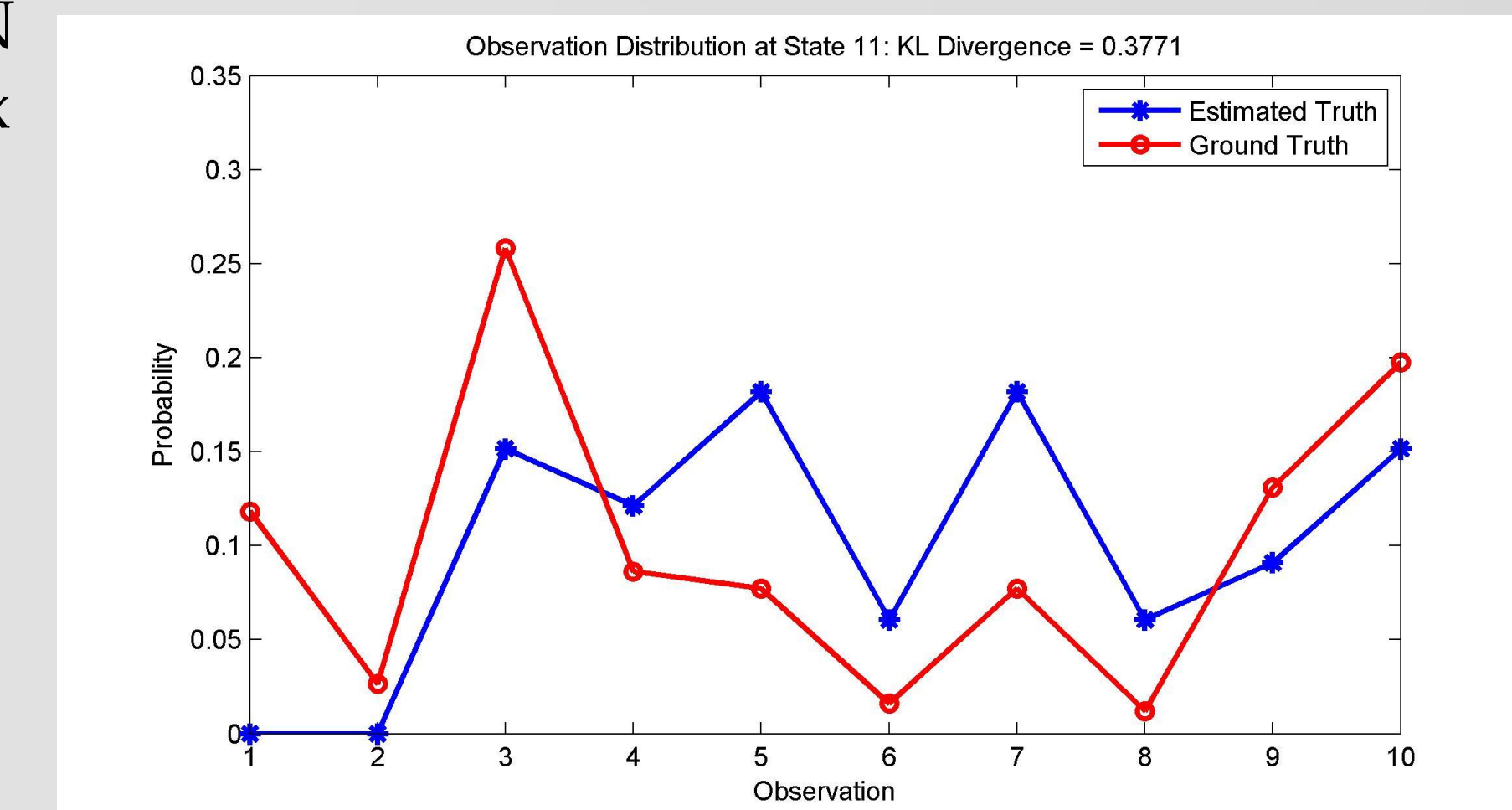
## Results

### Synthetic data

- Randomly generated N by N state transition matrix
  - Zero self transition
  - Row-wise normalization
  - N = 25 states
  - Duration = {1:4}
  - 1000 Time steps



- Randomly generated M by N observation transition matrix
  - M = 10 observations
  - Column-wise normalization



## Future Work

- Explore Explicit Duration Hidden Markov Models
  - The current method of parameter estimation requires a specified duration for all states
  - Implement Beam sampling to limit the number of states considered at each time step.
- Utilize feature vectors from an RGB camera to estimate model parameters.

## References

1. Rabiner, L.R., "A tutorial on hidden Markov models and selected applications in speech recognition," *Proceedings of the IEEE*, vol.77, no.2, pp.257-286, Feb 1989
2. Shun-Zheng Yu, "Hidden semi-Markov models", *Artificial Intelligence*, Volume 174, Issue 2, February 2010, Pages 215-243, ISSN 0004-3702, 10.1016/j.artint.2009.11.011.
3. Dewar, M.; Wiggins, C.; Wood, F., "Inference in Hidden Markov Models with Explicit State Duration Distributions," *Signal Processing Letters, IEEE*, vol.19, no.4, pp.235-238, April 2012
4. Jurgen Van Gael, Yunus Saatici, Yee Whye Teh, and Zoubin Ghahramani. "Beam sampling for the infinite hidden Markov model. In *Proceedings of the 25th international conference on Machine learning (ICML '08)*. ACM, New York, NY, USA, 1088-1095.